

# An Efficient Architecture for Ultra Long FFTs in FPGAs and ASICs

- Architecture optimized for Fast Ultra Long FFTs
- Parallel FFT structure reduces external memory bandwidth requirements
- Lengths from 32K to 256M
- Optimized for continuous data FFTs
- Architecture reduces the algorithm to two smaller manageable FFT engines



#### **Ultra Long FFTs**

- An FFT length that exceeds the internal memory requirements of the FPGA or ASIC
- System cost can be reduced in moderate length FFTs in designs where the FPGA/ASIC size is driven by the memory requirements.
- This architecture puts most of the storage for the FFT off chip in relatively inexpensive SRAM, reducing the system cost.
- Ultra Long FFTs have a similar structure to 2D FFTs
- Cooley-Tukey algorithm
- Minimizes external memory IC count and bandwidth



### What Ultra Long FFTs Need

The following shows the execution unit (logic) and memory requirement for continuous data FFTs of two lengths:

	1K	1M
Butterflies	10	20
Memory	2K	2M

- The logic requirements for a 1M FFT are only double a 1K FFT, while the memory requirements are 1000 times.
- Logic for 1M FFT easily fits into large FPGA
- Memory requirements exceed what is available even in a large FPGA



# Computing $N = N_1 \times N_2$

The  $N_1 \times N_2$  FFT can be computed as:

$$X[k_1N_2+k_2] = \sum_{n_1=0}^{N_1-1} \left[ e^{-j\frac{2\pi n_1k_2}{N}} \left( \sum_{n_2=0}^{N_2-1} x[n_2N_1+n_1] e^{-j\frac{2\pi n_1k_2}{N_2}} \right) \right] e^{-j\frac{2\pi n_1k_1}{N_1}}$$

Computing this for:

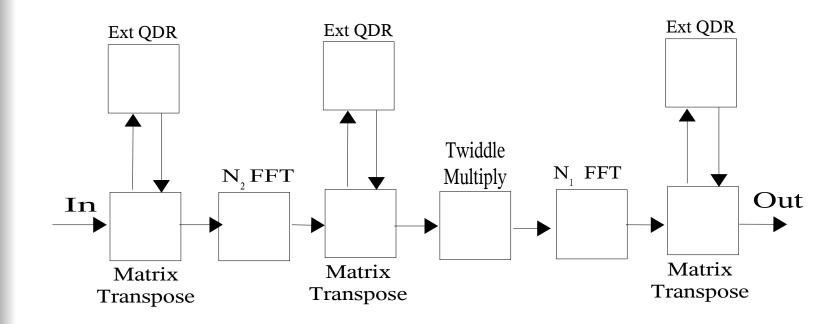
 $0 \leq k_1 \leq N_1 - 1$  and  $0 \leq k_2 \leq N_2 - 1$ 

**Results in:** 

$$X[k] = \sum_{n=0}^{N-1} x[n] e^{-j\frac{2\pi nk}{N}} \quad \text{for} \quad 0 \le k \le N-1, \quad \text{as desired}$$



## $N = N_1 \times N_2$ Architecture



- Three banks of external QDR Memory (single copy each)
- Two continuous data FFTs (N<sub>1</sub>, N<sub>2</sub>) inside FPGA
- Twiddle Multiply provides vector rotation between N<sub>2</sub> and N<sub>1</sub> FFTs.
- Final matrix transpose for normal order output.



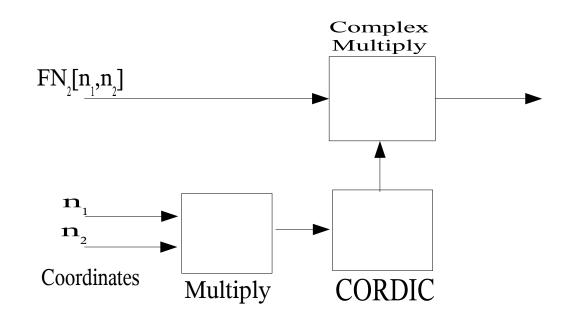
#### QDR SRAM

- Simultaneous read/writes (separate address/data bus) allow single bank of memory per memory transpose.
- DDR Style I/O so dual clock edge transfer with FPGA results in narrower data path.
- Single copy can be kept at each stage while maintaining continuous data flow.
- Special address sequence employed so data isn't overwritten in continuous data application. Reduce IC count.
- QDR with Virtex II Pro I/O up to 150MHz (read/write)
- QDR II with Virtex II Pro I/O up to 200MHz (read/write)



#### **CORDIC For Twiddle Factors Generation**

- Almost N/2 twiddle factors required.
- Very large ROM for FPGA or ASIC.
- CORDIC a natural fit, use coordinate product as input.



CORDIC produces the sin/cos terms for angle input.



#### Matrix Transpose Address Sequence

- Allows single copy for each matrix transpose.
- Operates on continuous data, one point read/written per clock cycle.
- Reduces memory IC count.
- Simple logic for sequence generation.
- Works for square or rectangular matrices.
- Sequence repeats after log<sub>2</sub>(N) sets.
- Write always follows read.
- Simple  $N = N_1 \times N_2 = 8$  example:

1 <sup>st</sup>	2 <sup>nd</sup>	3rd	1 <sup>st</sup>
0	0	0	0
1	2	4	1
2	46	1	2
2	6	5	234
4	1	2	4
5	3	6	5
5 6 7	3 5	5 2 6 3	56
7	7	$\overline{Z}$	7

 First and last matrix transpose go left to right in table, second right to left.



#### **Fixed vs. Floating Point**

- Numbers in radix-2 FFT can grow by log<sub>2</sub>(N), or 1 bit per butterfly rank.
- A 1M FFT can have 20 bits of growth. With 16 bit inputs results would be 36 bits.
- Scaling always required in fixed point versions.
- Fixed point scaling should be limited to every to every other rank, so 10 times for a 1M FFT producing 26 bit results from 16 bit input.
- Floating point FFT maintains precision without overflowing.
- Floating Point FFT uses approximately 8 times the logic of a similar precision fixed point version.



#### Virtex II Pro Performance – 512K FFT

- 80MHz Continuous Data
- 1K FFT Engine 4 butterflies
- 512 FFT Engine 4 butterflies
- FFT Engines at 160MHz
- QDR memory at 80MHz
- Real 14 bit input, complex 24 bit output
- Virtex II Pro Device Usage
  - Slices 12,500
  - BlockRAM 144
  - MULT18x18 88
- Fits in XC2VP40



#### **Other Uses of Architecture**

- 2D FFT Remove first matrix transpose and twiddle multiply.
- Variable Length Use variable length FFTs and dynamic matrix transpose blocks.
- Mixed Radix FFTs Substitute other than radix-2 for 2<sup>nd</sup> FFT.
- Performance increases easy with parallel input radix-2 FFTs and multiple paths to SRAM.



### **Other Dillon Engineering Resources**

- ParaCore Architect (parameterized core builder)
- DSP Algorithms
  - Mixed radix FFTs
  - 2D FFTs for image processing
  - Fixed or floating-point FFTs
  - Floating point math library
  - AES Cryptography
- System level DSP
  - OFDM Transceivers
  - Radar Processing on single FPGA
  - Image Compression/Processing
- Hardware/Software SOC
  - High speed Ethernet Appliances
  - Linux Based SOC in FPGA
  - MicroBlaze application